

# Relationship between Cycle Time and Setup Value in Single type Preventive Maintenance Scheduling

xS3D. Minho, Lee

# Contents

(1) Introduction

(2) System description

① New trade-off

② The queueing networks with single PM

③ The queueing networks with multiple PMs

(3) Relation between Cycle Time and Setup value

(4) Relation between Cycle of  $PM(m_T)$  and Setup value

(5) Conclusion and future task

# (1) Introduction

- What is the PM?

- PM is abbreviation of Preventive Maintenance.
- Maintaining equipment and facilities in satisfactory operating condition by providing for systematic inspection, detection.
- Primary goal is to avoid or mitigate the consequences of failure of equipment.
- In brief, **periodic unproductive examination** of equipment before use it.

# (1) Introduction

- What is the PM?

## Automobile

- Oil changes are part of a car's preventive maintenance.

→ Preventing a car from being stopped unexpectedly.

## Train

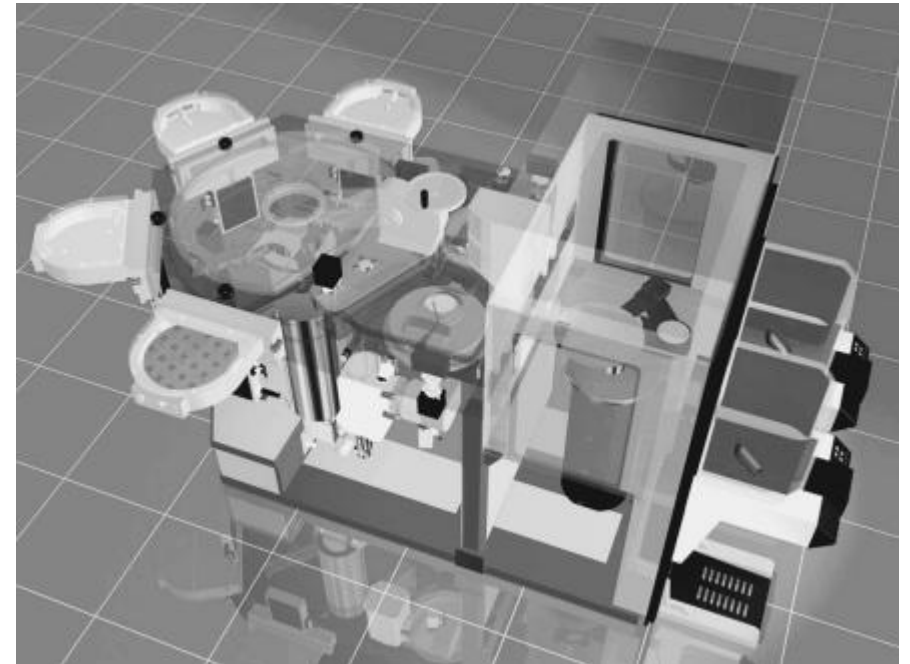
- Preventive maintenance on railroad tracks.

→ Preventing a train derailment resulting in damage of human life.



# (1) Introduction

- PM in semiconductor manufacturing equipment
  - PM activities are more complex and essential than any other manufacturing system.
  - Thus, PM tasks have to be scheduled carefully.



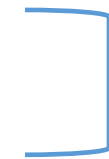
# (1) Introduction

- Why we need a good PM plan?

- A good PM plan can increase equipment availability.

- Occurring **planned downtime** due to PM.

- But preventing a risk of costly **unplanned downtime** due to equipment failure.



Existing trade-off

- Overall equipment availability 

- Equipment reliability 

# (1) Introduction

- What we have to do

- Consider queueing system in the production process,

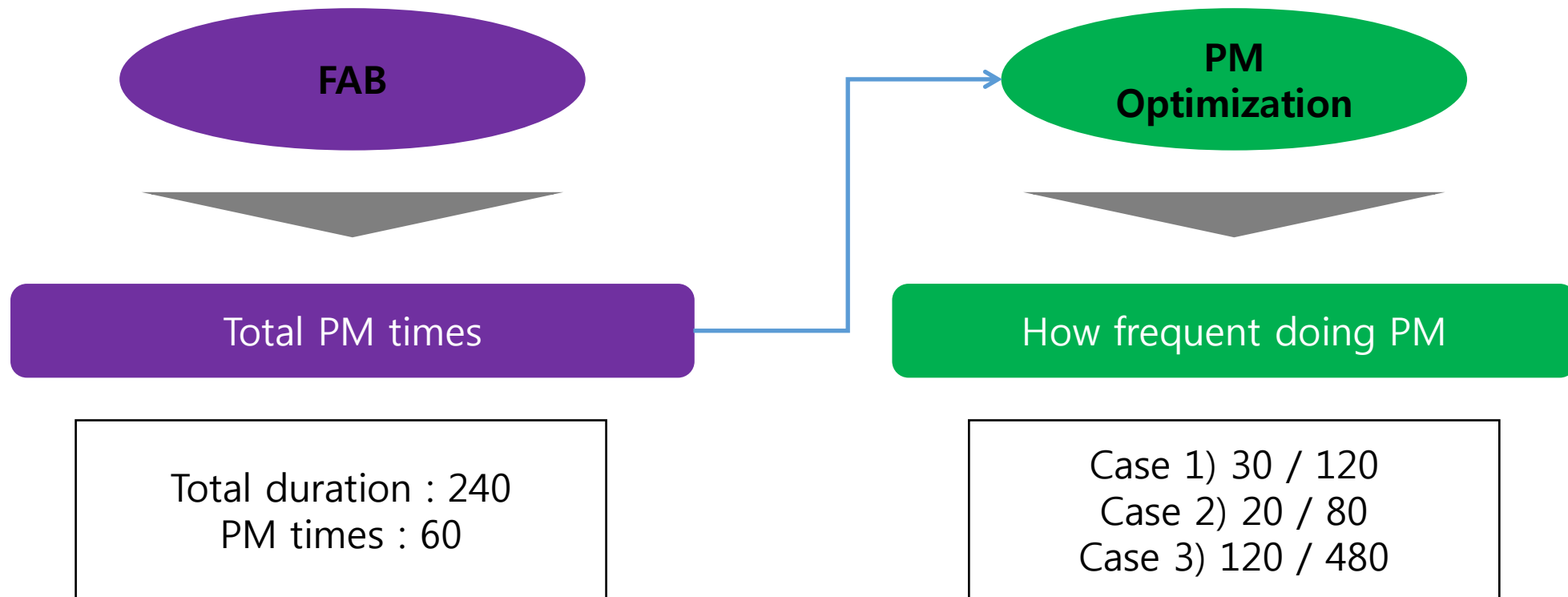
- We want to minimize cycle time in queueing system

- When the original PM plan is given from fab, we can change the PM cycle in accordance with the PM type.

- PM times of total cycle is determined by fab, we just determine when or how frequent we do PM.

# (1) Introduction

- What we have to do





# (2) System description

## ① New trade-off

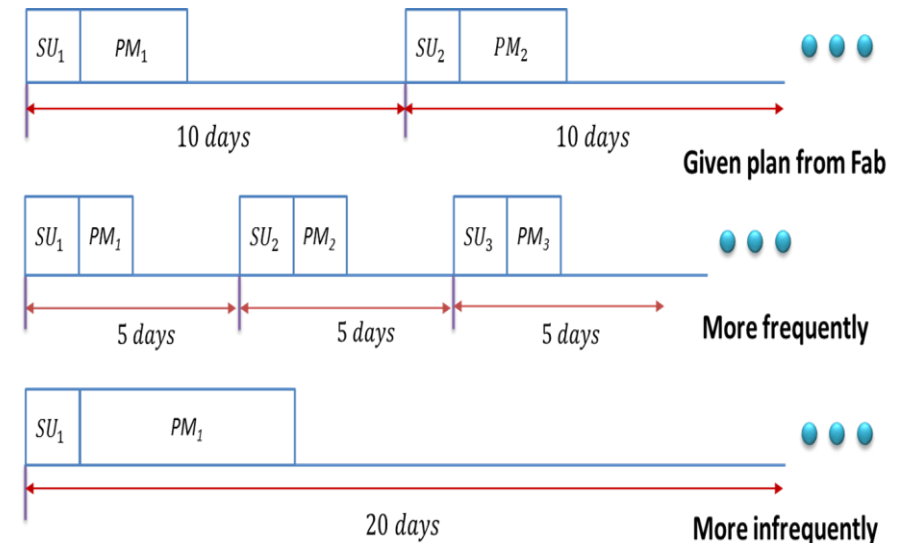
- Even though the PM cycle is change, the setup time is fixed.

1) More frequent PM : Total incurred setup times  $\uparrow$

→ Availability  $\downarrow$  , mean time to repair  $\downarrow$

2) More infrequent PM : Total incurred setup times  $\downarrow$

→ Availability  $\uparrow$  , mean time to repair  $\uparrow$



## (2) System description

### ① New trade-off

$$E(CT) = \frac{1}{\mu A} + \frac{1}{\mu A} \left( \frac{\rho}{1-\rho} \right) \left( \frac{1}{2} \right) \left( 1 + C_S^2 + \frac{(1 + C_R^2) A (1-A) m_R \mu}{\rho} \right)$$

Factory Physics Mean Cycle  
Time formula

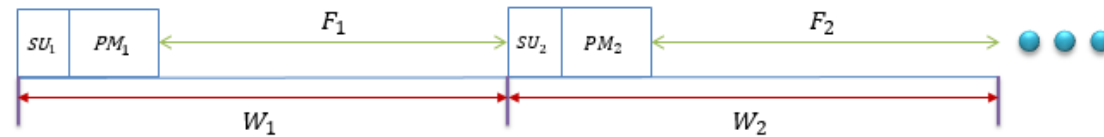
- Frequent case : Availability (A) ↓
- Frequent case : mean time to repair ( $m_R$ ) ↓

- Infrequent case : Availability (A) ↑
- Infrequent case : mean time to repair ( $m_R$ ) ↑

Existing trade-off

## (2) System description

### ② Queueing networks of single type of PM

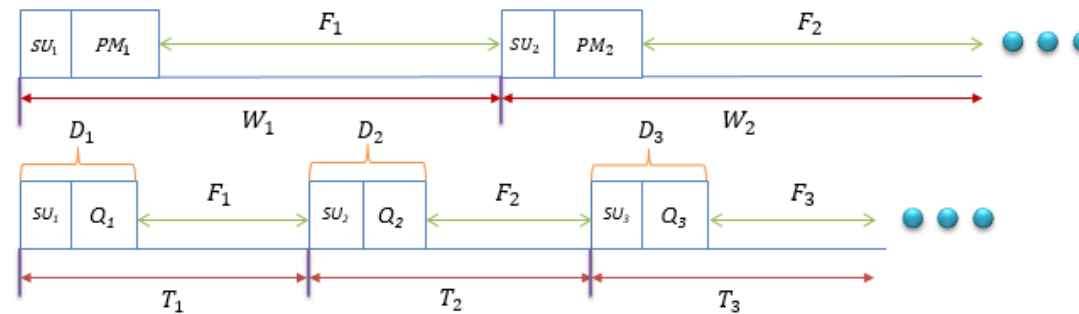


- Four random variables

- $\{F_j\}_{j=1}^{\infty}$  denote IID random variables of the  $j^{th}$  duration of uptimes.
- $\{PM_j\}_{j=1}^{\infty}$  denote IID random variables of the  $j^{th}$  preventive maintenance.
- $\{SU_j\}_{j=1}^{\infty}$  denote IID random variables of the  $j^{th}$  setup times. where  $SU_j = \frac{PM_j}{k_j}$
- $\{W_j\}_{j=1}^{\infty}$  denote IID random variables of the  $j^{th}$  total duration ( $W_j = F_j + PM_j + SU_j$ ).

# (2) System description

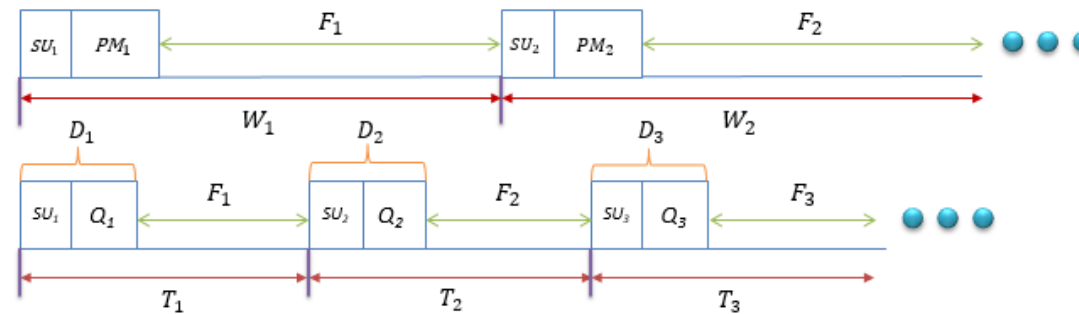
## ② Queueing networks of single type of PM



- Original plan and Changed PM plan
  - $m_W$ : The mean time of total duration of Original plan
  - $m_T$ : The mean time of the changed PM cycle.
  - $m_T$  is decision variable.  $L \leq m_T \leq U$

## (2) System description

### ② Queueing networks of single type of PM



- $m_R(m_T) = \left( \frac{1}{k_j} + \frac{m_T}{m_w} \right) E[PM] = E[SU] + E[Q], \quad C_R^2 = C_{PM}^2$
- $m_F(m_T) = m_T - m_R, \quad F_i \sim \text{Exp}\left(\frac{1}{m_F(m_T)}\right) \text{ IID}$
- $A(m_T) = \frac{m_F}{m_F + m_R}$  (Availability),  $\rho(m_T) = \frac{\lambda}{\mu A(m_T)}$  (System loading).

## (2) System description

### ② Queueing networks of single type of PM

- Nonlinear programming problem
- M/G/1-queue case

$$\text{Min } CT(m_T)$$

Subject to

$$m_T > \frac{m_{SU}m_w}{(m_w*(1-\lambda/\mu)-m_{PM})} \text{ (system loading constraint)}$$

$$L \leq m_T \leq U$$

$$E(CT) = \frac{1}{\mu A} + \frac{1}{\mu A} \left( \frac{\rho}{1-\rho} \right) \left( \frac{1}{2} \right) \left( 1 + C^2_S + \frac{(1 + C^2_R)A(1-A)m_R\mu}{\rho} \right)$$

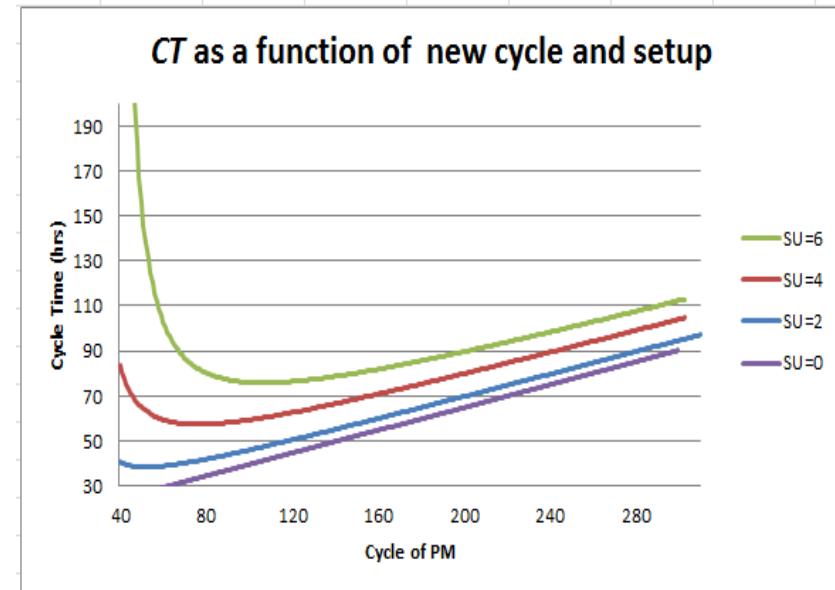
# (3) Relation between Cycle Time and Setup Value

- In Hungil's thesis

- Setup time is given parameter.
- Decision variable : Cycle of PM ( $m_T$ )
- Objective : Cycle time ( $E(CT)$ )

→ Function of cycle time according to cycle of PM is strictly convex.

→ So we can calculate optimal cycle time easily.



# (3) Relation between Cycle Time and Setup Value

- Research goal

- Setup value is a given parameter.
- We observe change of the optimal cycle time according to changing setup value.
- If the relation between optimal cycle time and setup value is linear, optimal cycle time is

easier to calculate.

$$E(CT) = \alpha * m_T + \beta$$



# (3) Relation between Cycle Time and Setup Value

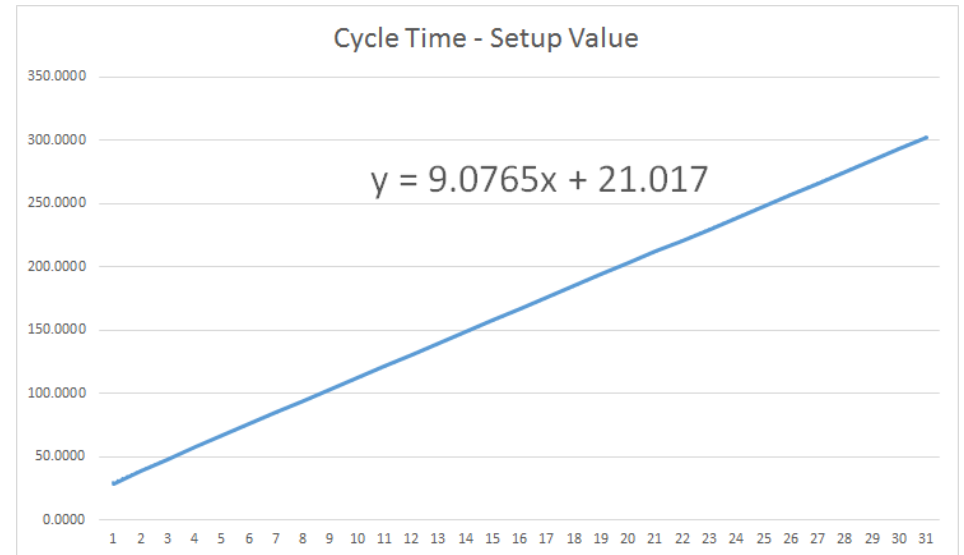
- How to prove
  - Optimal cycle time : Using Excel solver
  - Observe regression line of cycle time and setup time.

- First case : Change setup value from 1 to 30 (∵ Cycle of PM have bounds)
- Second case : Change setup value from 0.1 to 2

# (3) Relation between Cycle Time and Setup Value

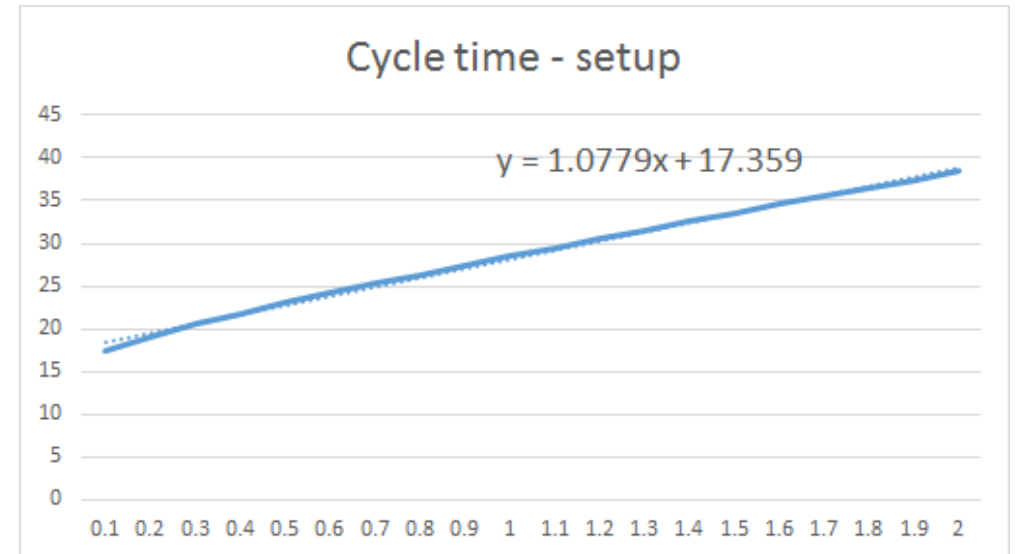
- First case (From 1 to 30)

- Observe the error between optimal value and value of the regression line.
- The error at lower setup values(1~2) between optimal value by using Excel solver and value of regression line are a little bigger than higher setup values.



# (3) Relation between Cycle Time and Setup Value

- Second case (From 0.1 to 2)
  - To observe more accurate, change the range of setup value from 0.1 to 2.
  - More clear that the relation is not linear.
  - Similar to linear, not perfect linear



# (4) Relation between the cycle of $PM(m_T)$ and Setup Value

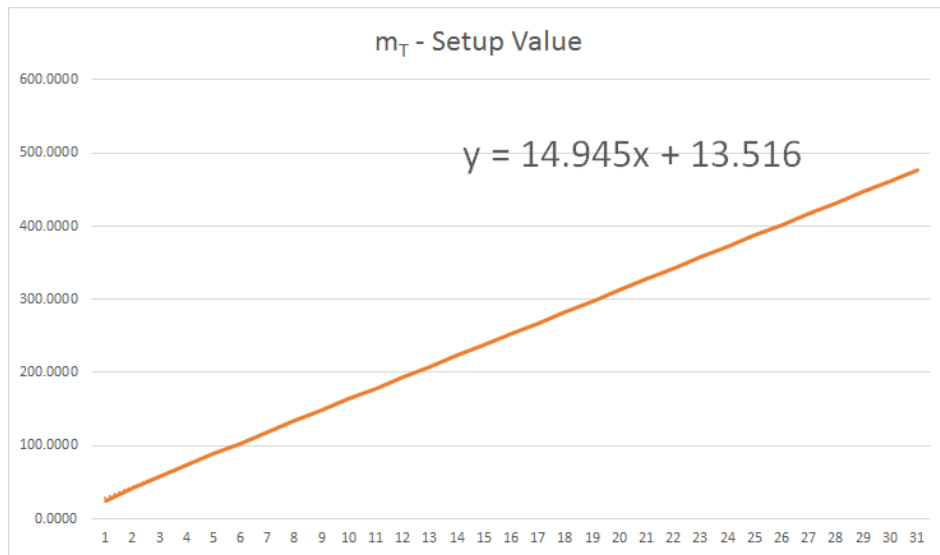
- How to prove

- Similar to previous case.

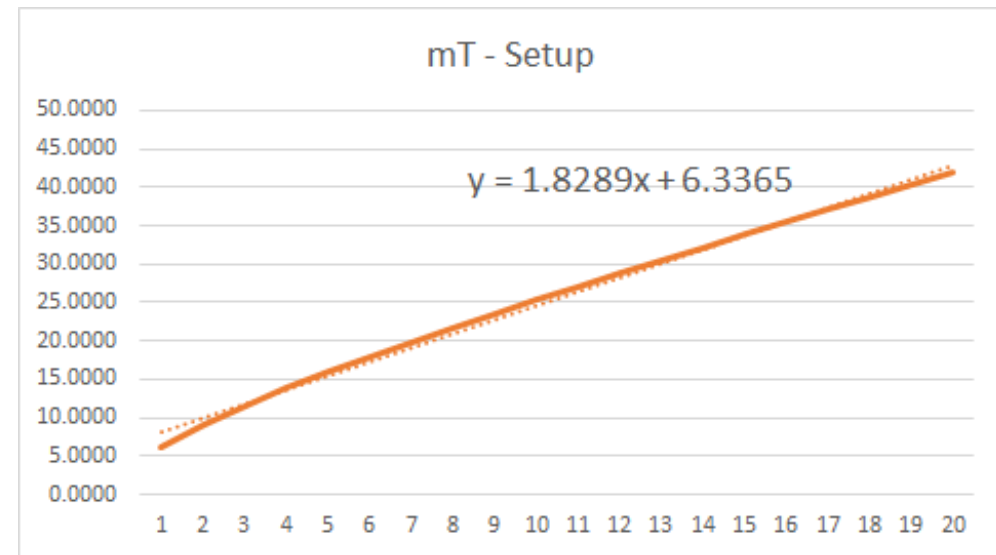
- First case : Change setup value from 1 to 30 ( $\because$  Cycle of PM have bounds)
- Second case : Change setup value from 0.1 to 2

# (4) Relation between the cycle of $PM(m_T)$ and Setup Value

- First case (From 1 to 30)



- Second case (From 0.1 to 2)



→ Same results with previous case.

# (5) Conclusion and future task

- Conclusion & Future task

- Relation between cycle time(or PM cycle) and setup value is not perfect linear.
- If we know the exact relation between cycle time and setup value and if we can express the relation using the simple formula, calculating cycle time with incurred setup value becomes easier.

# (5) Conclusion and future task

- Dominance property
  - If there are two types of PM.
  - One is more influential to cycle time.
  - And we have to choose type of PM which is rescheduled preferentially.
  - Thus we need the rule of thumb.

